

1 Data Structures

Give a tight asymptotic bound for each of the following problems. Provide your bound in $\Theta(\cdot)$ if it exists, otherwise provide both the $O(\cdot)$ and $\Omega(\cdot)$ bound.

- 1.1 Insertion of one element into each of the following data structures where N is the number of elements already in the collection.
 - (a) ArrayList
 - (b) LinkedList
 - (c) BSTMap (binary search tree)
 - (d) TreeSet (balanced search tree)
 - (e) HashSet
- 1.2 Containment check (contains) of one element in each of the following data structures where N is the number of elements already in the collection.
 - (a) ArrayList
 - (b) LinkedList
 - (c) BSTMap (binary search tree)
 - (d) TreeSet (balanced search tree)
 - (e) HashSet
- 1.3 Suppose we're designing a hash table. Compare and contrast each of the following external chaining implementations. Why would you use one over the other?
 - (a) Linked list

 - (b) Resizing array

 - (c) Balanced search tree

 - (d) Hash table

2 Hash Codes

There is a problem with each hashCode() method below (correctness, distribution, efficiency). Assume there are no problems with the correctness of equals().

```

2.1 class PokeTime {
    int startTime;
    int duration;
    public int getCurrentTime() {
        // Gets the current system clock time
    }
    public int hashCode() {
        return 1021 * (startTime + 1021 * duration + getCurrentTime());
    }
    public boolean equals(Object o) {
        PokeTime p = (PokeTime) o;
        return p.startTime == startTime && p.duration == duration;
    }
}

2.2 class Phonebook {
    List<Human> humans;
    public int hashCode() {
        int h = 0;
        for (Human human : humans) {
            // Assume Human::hashCode is correct
            h = (h + human.hashCode()) % 509;
        }
        return h;
    }
    public boolean equals(Object o) {
        Phonebook p = (Phonebook) o;
        return p.humans.equals(humans);
    }
}

2.3 class Person {
    Long id;
    String name;
    Integer age;
    public int hashCode() {
        return id.hashCode() + name.hashCode() + age.hashCode();
    }
    public boolean equals(Object o) {
        Person p = (Person) o;
        return p.id == id;
    }
}

```